

# ΕΠΛ323 - Θεωρία και Πρακτική Μεταγλωττιστών

Lecture 6a

## **Syntax Analysis**

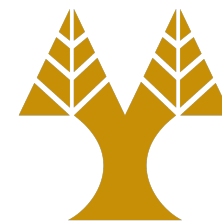
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# Top-Down Parsing



- Can be viewed as an attempt to find a leftmost derivation for an input string
- May involve **backtracking**
  - Use left-factoring to remove backtracking
- Two types of parsers
  - **Non recursive predictive parsing** is table driven
  - **Recursive-descent parsing**, where a procedure is associated with each non-terminal symbol

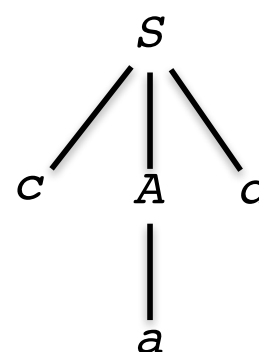
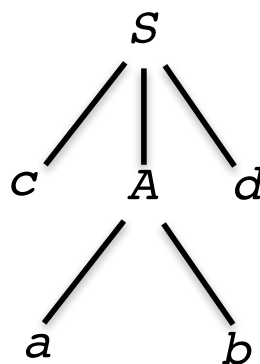
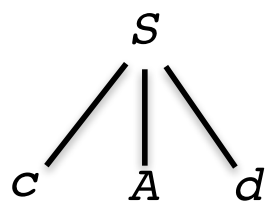
# Backtracking



$S \rightarrow cAd$

$A \rightarrow ab \mid a$

*Consider the input string  $w=cad$*

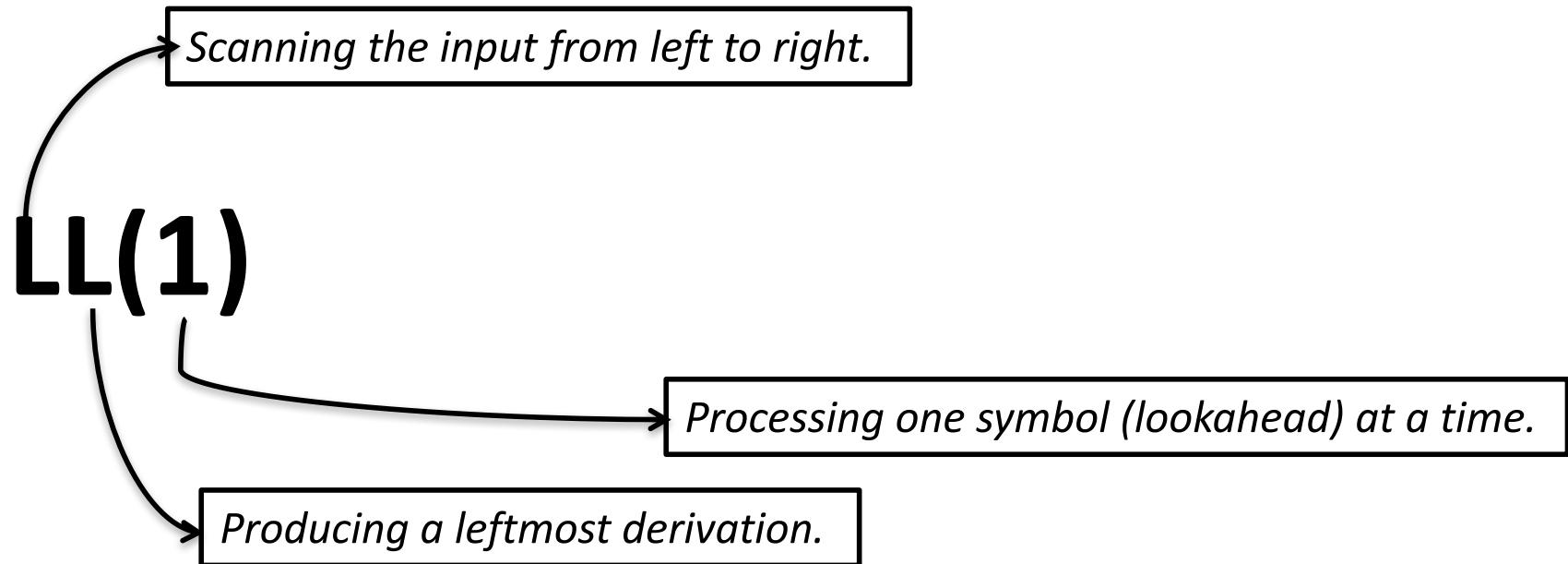


# Predictive parsing

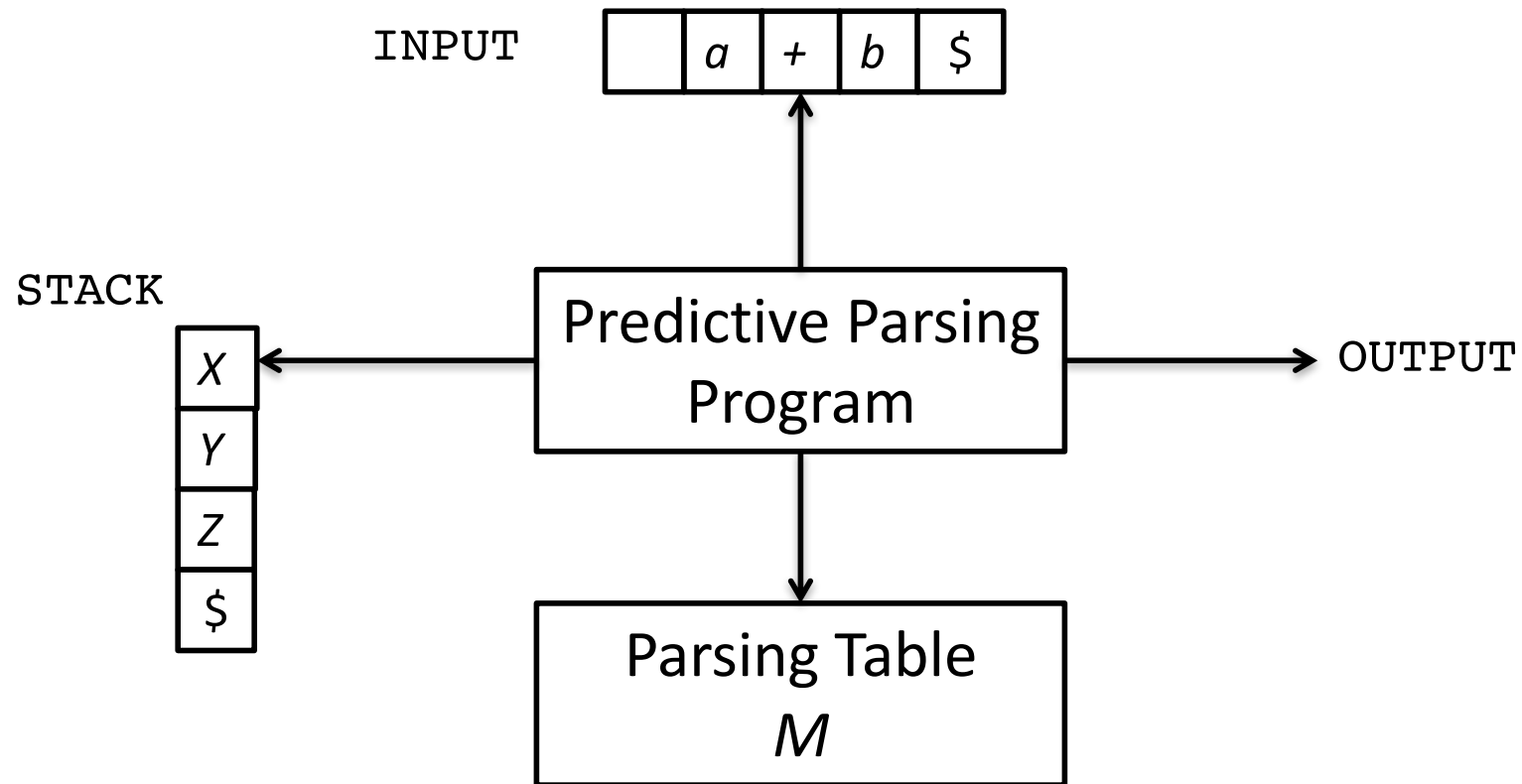
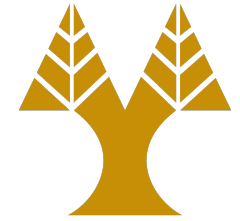


- If we carefully re-write the grammar by eliminating left recursion and by left factoring the grammar, then the result can be parsed with no backtracking

```
stmt → if expr then stmt else stmt  
      | while expr do stmt  
      | begin stmt_list end
```



# Non recursive predictive parser



$\$$ : end symbol

$X, Y, Z$ : non-terminals or terminals

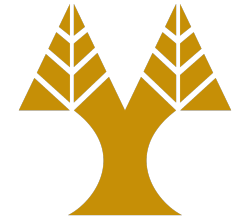
# Parsing Table $M$



NONTERMINAL	INPUT SYMBOL					
	id	+	*	(	)	\$
$E$	$E \rightarrow TE'$			$E \rightarrow TE'$		
$E'$		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
$T$	$T \rightarrow FT'$			$T \rightarrow FT'$		
$T'$		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
$F$	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

$E$	$\rightarrow$	$TE'$	
$E'$	$\rightarrow$	$+TE'$	$\mid \epsilon$
$T$	$\rightarrow$	$FT'$	
$T'$	$\rightarrow$	$*FT'$	$\mid \epsilon$
$F$	$\rightarrow$	$(E)$	$\mid \text{id}$

# Stack for **id + id\*id**



STACK	INPUT	OUTPUT
\$E	id + id * id\$	
\$E'T	id + id * id\$	$E \rightarrow TE'$
\$E'T'F	id + id * id\$	$T \rightarrow FT'$
\$E'T'id	id + id * id\$	$F \rightarrow id$
\$E'T'	+ id * id\$	
\$E'	+ id * id\$	$T' \rightarrow \epsilon$
\$E'T+	+ id * id\$	$E' \rightarrow +TE'$
\$E'T	id * id\$	
\$E'T'F	id * id\$	$T \rightarrow FT'$
\$E'T'id	id * id\$	$F \rightarrow id$
\$E'T'	* id\$	
\$E'T'F*	* id\$	$T' \rightarrow *FT'$
\$E'T'F	id\$	
\$E'T'id	id\$	$F \rightarrow id$
\$E'T'	\$	
\$E'	\$	$T' \rightarrow \epsilon$
\$	\$	$E' \rightarrow \epsilon$



# FIRST ( )



If  $a$  is any string of grammar symbols, let  $FIRST(a)$  be the set of terminals that begin the strings derived from  $a$ .

- Rule 1
  - If  $X$  is a terminal then  $FIRST(X) = \{X\}$
- Rule 2
  - If  $X \rightarrow \epsilon$ , then we add  $\{\epsilon\}$  to  $FIRST(X)$ .
- Rule 3
  - If  $X$  is nonterminal, and  $X \rightarrow Y_1 Y_2 \dots Y_m$  then add  $FIRST(Y_1 Y_2 \dots Y_m)$  to  $X$ 
    - $FIRST(Y_1)$  if  $FIRST(Y_1)$  does not contain  $\epsilon$
    - $FIRST(Y_1)$  and  $FIRST(Y_2 \dots Y_m)$  (excluding  $\epsilon$ ) if  $FIRST(Y_1)$  contains  $\epsilon$
    - If  $FIRST(Y_m)$  contains  $\epsilon$ , then add also  $\epsilon$

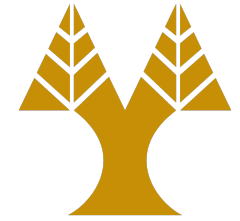
# Example



$E$	$\rightarrow$	$TE'$	
$E'$	$\rightarrow$	$+TE' \mid \varepsilon$	
$T$	$\rightarrow$	$FT'$	
$T'$	$\rightarrow$	$*FT' \mid \varepsilon$	
$F$	$\rightarrow$	$(E) \mid \mathbf{id}$	

$\text{FIRST}(+)$	$=\{+\}$
$\text{FIRST}(*)$	$=\{*\}$
$\text{FIRST}(())$	$=\{($
$\text{FIRST}( ) )$	$=\{)\}$
$\text{FIRST}(\mathbf{id})$	$=\{\mathbf{id}\}$
$\text{FIRST}(E)$	$=\{(, \mathbf{id}\}$
$\text{FIRST}(T)$	$=\{(, \mathbf{id}\}$
$\text{FIRST}(F)$	$=\{(, \mathbf{id}\}$
$\text{FIRST}(E')$	$=\{+, \varepsilon\}$
$\text{FIRST}(T')$	$=\{*, \varepsilon\}$

# FOLLOW ( )



$FOLLOW(A)$ , for a nonterminal  $A$ , is the set of terminals  $a$  that can appear immediately to the right of  $A$ .

- Rule 1
  - Add  $\$$  to the follow set of the starting symbol.
- Rule 2
  - If  $A \rightarrow aBb$ , then  $FOLLOW(B)$  contains at least  $FIRST(b)$  (with  $\epsilon$  excluded)
- Rule 3
  - If  $(A \rightarrow aB)$  or  $(A \rightarrow aBb \text{ and } \epsilon \text{ is in } FIRST(b))$  then  $FOLLOW(A)$  contains at least  $FOLLOW(B)$

# Example



$E$	$\rightarrow$	$TE'$	
$E'$	$\rightarrow$	$+TE' \mid \varepsilon$	
$T$	$\rightarrow$	$FT'$	
$T'$	$\rightarrow$	$*FT' \mid \varepsilon$	
$F$	$\rightarrow$	$(E)$	<b>id</b>

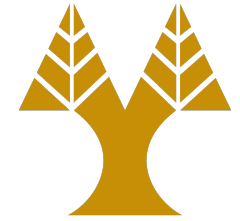
$\text{FOLLOW}(E)$	$= \{ ), \$ \}$
$\text{FOLLOW}(E')$	$= \{ ), \$ \}$
$\text{FOLLOW}(T)$	$= ( + , ) , \$ )$
$\text{FOLLOW}(T')$	$= ( + , ) , \$ )$
$\text{FOLLOW}(F)$	$= ( * , + , ) , \$ )$

# Constructing the parsing table



1. For each  $A \rightarrow a$  production of the grammar, do steps 2 and 3.
2. For each terminal  $a$  in  $FIRST(a)$ , add  $A \rightarrow a$  to  $M[A, a]$ .
3. If  $\epsilon$  is in  $FIRST(a)$ , add  $A \rightarrow a$  to  $M[A, b]$  for each terminal  $b$  in  $FOLLOW(A)$ . If  $\epsilon$  is in  $FIRST(a)$  and  $\$$  is in  $FOLLOW(A)$ , add  $A \rightarrow a$  to  $M[A, \$]$ .
4. Make each undefined entry of  $M$  be **error**.

# Error Recovery with Synchronizing Symbols



NONTERMINAL	INPUT SYMBOL					
	id	+	*	(	)	\$
$E$	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
$E'$		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
$T$		synch		$T \rightarrow FT'$	synch	synch
$T'$		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
$F$	$F \rightarrow \text{id}$	synch	synch	$F \rightarrow (E)$	synch	synch

$\text{FOLLOW}(E) = \{ ), \$ \}$

$\text{FOLLOW}(E') = \{ ), \$ \}$

$\text{FOLLOW}(T) = \{ +, ), \$ \}$

$\text{FOLLOW}(T') = \{ +, ), \$ \}$

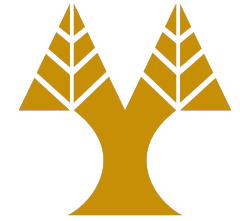
$\text{FOLLOW}(F) = \{ *, +, ), \$ \}$

# Stack for **id\*+id**



STACK	INPUT	OUTPUT
\$E	<b>id*+id</b> \$	
\$E'T	<b>id*+id</b> \$	
\$E'T'F	<b>id*+id</b> \$	
\$E'T'id	<b>id*+id</b> \$	
\$E'T'	<b>*+id</b> \$	
\$E'TF*	<b>*+id</b> \$	
\$E'TF	<b>+id</b> \$	synch, pop()
\$E'T'	<b>+id</b> \$	
\$E'	<b>+id</b> \$	
\$E'T+	<b>+id</b> \$	
\$E'T	<b>id</b> \$	
\$E'TF	<b>id</b> \$	
\$E'T'id	<b>id</b> \$	
\$E'T'	\$	
\$E'	\$	
\$	\$	

# Recursive Descent Example



```
type      → simple
            | ^id
            | array [simple] of type
simple    → integer
            | char
            | num dotdot num
```

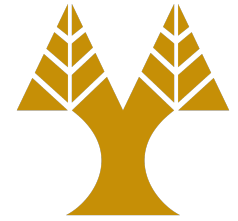


# match ( )



```
match(token t) {  
    // lookahead global variable  
    // with current token  
    if lookahead == t  
        then lookahead = getnext();  
    else  
        error();  
}
```

# simple()



```
simple() {  
    if lookahead == integer  
        match(integer);  
    else if lookahead == char  
        match(char);  
    else if lookahead == num {  
        match(num); match(dotdot); match(num);  
    }  
    else  
        error();  
}
```

# type()



```
type() {
    if (lookahead == integer ||
        lookahead == char ||
        lookahead == num)
        simple();
    else if (lookahead == '^') {
        match("^"); match(id);
    }
    else if (lookahead == array) {
        match(array);
        match('['); simple(); match(']');
        match(of); type();
    }
    else
        error();
}
```